

Date: 09/02/2020

Time allowed: 1:30 hrs

Answer ALL questions

$$DF = k_f \cdot \Delta m$$

$$DF = 3000 \times 2 = 6000$$

Question 1 [15 marks]

$$\beta_F = \frac{DF}{FM} = \frac{6000}{1000} = 6$$

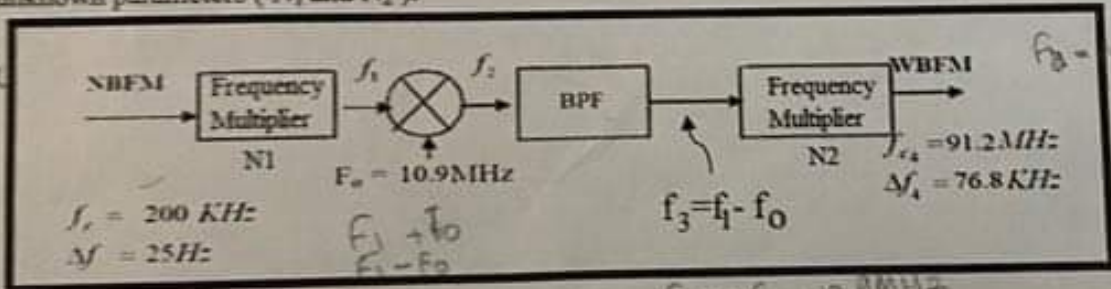
The carrier  $c(t) = A \cos 2\pi 10^6 t$  is angle modulated (PM or FM) by the sinusoid signal  $m(t) = 2 \cos 2000\pi t$ . The deviation constants are  $k_p = 1.5 \text{ rad/V}$  and  $k_f = 3000 \text{ Hz/V}$ .

1. Determine  $\beta_F$  and  $\beta_P$ . [4]
2. Determine the bandwidth in each case using Carson's rule. [2]
3. Plot the spectrum of the modulated signal in case of FM modulation. [5]
4. If the amplitude of  $m(t)$  is decreased by a factor of two, how would your answers to parts 1-2 change? [2]
5. If the frequency of  $m(t)$  is increased by a factor of two, how would your answers to parts 1-2 change? [2]

$$B_w = 2(1 + \beta) F_m =$$

Question 2 [10 marks]

Block diagram of an indirect (Armstrong) FM transmitter is shown below. Compute the unknown parameters ( $N_1$  and  $N_2$ ).



$$\frac{DF_n}{DF} = n_1 n_2 = 3072$$

$$n_1 = \frac{3072}{n_2}$$

$$3072 = \frac{3072}{n_2} \cdot n_2$$

$$f_3 = f_1 - 10.9 \text{ MHz}$$

$$f_3 = n_2 f_2 - f_0$$

$$91.2 \text{ MHz} = (N_1 \cdot 200000 - 10.9 \text{ MHz}) \cdot 41.24$$

Note: Table of Bessel function

$J_n(\beta)$	$\beta=1$	$\beta=2$	$\beta=3$	$\beta=4$	$\beta=5$	$\beta=6$
$n=0$	0.7652	0.2239	-0.2601	-0.3971	-0.1776	0.1506
$n=1$	0.4401	0.5767	0.3391	-0.0660	-0.3276	-0.2767
$n=2$	0.1149	0.3528	0.4861	0.3641	0.0466	-0.2429
$n=3$	0.0196	0.1289	0.3091	0.4302	0.3648	0.1148
$n=4$	0.0025	0.0340	0.1320	0.2811	0.3912	0.3576
$n=5$	0.0002	0.0070	0.0430	0.1321	0.2611	0.3621
$n=6$	0.0000	0.0012	0.0114	0.0491	0.1310	0.2458
$n=7$	0.0000	0.0002	0.0025	0.0152	0.0534	0.1296
$n=8$	0.0000	0.0000	0.0005	0.0040	0.0184	0.0565
$n=9$	0.0000	0.0000	0.0001	0.0009	0.0055	0.0212
$n=10$	0.0000	0.0000	0.0000	0.0002	0.0015	0.0070

$$\frac{200}{n_1} = f_1 \Rightarrow$$

**Question 1 [15 marks]**

A carrier signal  $A_c \cos(\omega_c t)$  is modulated by a signal  $m(t) = A_m \cos(\omega_m t)$  to form an AM modulated signal  $s(t) = [A_c + A_m \cos(\omega_m t)] \cos(\omega_c t)$ , where  $A_c = 10$ ,  $A_m = 2$ ,  $f_c = 1000\text{Hz}$ ;  $f_m = 50\text{Hz}$ .

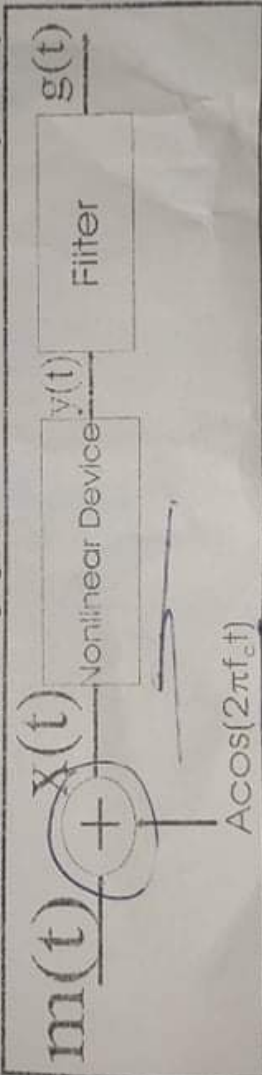
- Obtain the expressions for the sidebands of  $s(t)$ . [2 marks]
- Sketch the spectra  $M(f)$ ,  $C(f)$  and  $S(f)$  against  $f$ . [3 marks]
- Calculate the modulation index  $(\mu)$ . [4 marks]
- What bandwidth is required to transmit AM signal? [2 marks]
- Show that the total sideband power to the total power in the modulated wave is equal to  $\mu^2 / (\mu^2 + 2)$ . [2 marks]

**Question 2 [10 marks]**

(1) The DSB-SC signal is  $r(t) = m(t)\cos(2\pi f_c t)$  is applied to the input of a coherent detector, the local oscillator used in coherent detector is defined by  $c_p(t) = \cos(2\pi f_c t + \theta)$ . The output of the coherent detector is then filtered to obtain the baseband signal.

- Write the expression of the output waveform. [3 marks]
- Discuss the effect of this phase shift. [2 marks]

(2) Consider the system in the following figure.



Assume that the non linear device has the input-output relationship of the form

$$y(t) = a_1 x(t) + a_2 x^2(t)$$

And  $|m(t)| \leq 1$ , the bandwidth of  $m(t)$  is  $w$

- Write the equation for  $x(t)$
- Write the equation for  $y(t)$
- Describe the filter that yield an AM signal for  $g(t)$
- Write the equation for  $g(t)$ .
- Find the condition of  $a_1$  and  $a_2$  such that the signal generated  $g(t)$  is not over-modulated

**Notes**

$$\begin{aligned} \sin(x-y) &= \sin(x)\cos(y) - \cos(x)\sin(y) \\ \cos(x+y) &= \cos(x)\cos(y) - \sin(x)\sin(y) \\ \cos(x)\cos(y) &= \frac{1}{2}[\cos(x-y) + \cos(x+y)] \\ \sin(x)\sin(y) &= \frac{1}{2}[\cos(x-y) - \cos(x+y)] \end{aligned}$$